

- 1 $f(x) = |2x + 3| - 4, x \in \mathbb{R}$
 - a Sketch the graph of $y = f(x)$, labelling its vertex and any points of intersection with the coordinate axes. (5 marks)
 - b Find the coordinates of the points of intersection of $y = |2x + 3| - 4$ and $y = -\frac{1}{4}x + 2$ (5 marks)

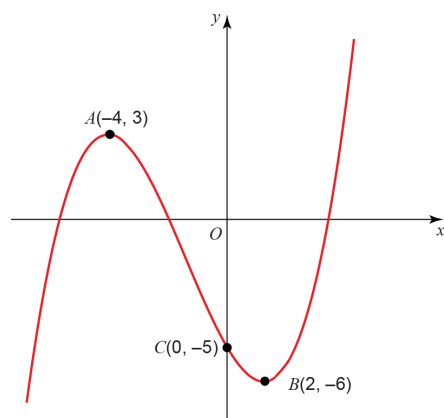
- 2 The functions p and q are defined by $p: x \rightarrow x^2$ and $q: x \rightarrow 5 - 2x$
 - a Given that $pq(x) = qp(x)$, show that $3x^2 - 10x + 10 = 0$ (4 marks)
 - b Explain why $3x^2 - 10x + 10 = 0$ has no real solutions. (2 marks)

- 3 The functions f and g are defined by $f(x) = e^{2x} + 4, x \in \mathbb{R}$ and $g(x) = \ln(x + 1), x \in \mathbb{R}, x > -1$
 - a Find $fg(x)$ and state its range. (4 marks)
 - b Solve $fg(x) = 85$ (3 marks)

- 4 The function $g(x)$ is defined by $g(x) = x^2 - 8x + 7, x \in \mathbb{R}, x > 4$. Find $g^{-1}(x)$ and state its domain and range. (6 marks)

- 5 The diagram shows the graph of $h(x)$.

Figure 1



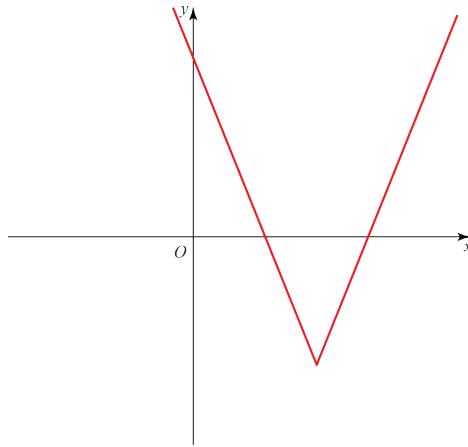
The points $A(-4, 3)$ and $B(2, -6)$ are turning points on the graph and $C(0, -5)$ is the y -intercept. Sketch on separate diagrams, the graphs of

- a $y = |f(x)|$ (3 marks)
- b $y = f(|x|)$ (3 marks)
- c $y = 2f(x + 3)$ (3 marks)

Where possible, label clearly the transformations of the points A , B and C on your new diagrams and give their coordinates.

- 6 The diagram shows a sketch of part of the graph $y = f(x)$ where $f(x) = 3|x - 4| - 5$

Figure 2



- a State the range of f . **(1 mark)**
- b Given that $f(x) = -\frac{1}{3}x + k$, where k is a constant has two distinct roots, state the possible values of k . **(7 marks)**
- 7 The temperature of a mug of coffee at time t can be modelled by the equation $T(t) = T_R + (90 - T_R)e^{-\frac{1}{20}t}$, where $T(t)$ is the temperature, in $^{\circ}\text{C}$, of the coffee at time t minutes after the coffee was poured into the mug and T_R is the room temperature in $^{\circ}\text{C}$.
- a Using the equation for this model, explain why the initial temperature of the coffee is independent of the initial room temperature. **(2 marks)**
- b Calculate the temperature of the coffee after 10 minutes if the room temperature is 20°C . **(2 marks)**