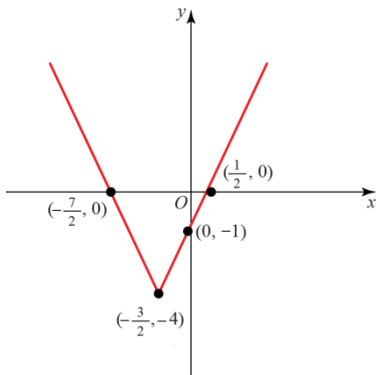
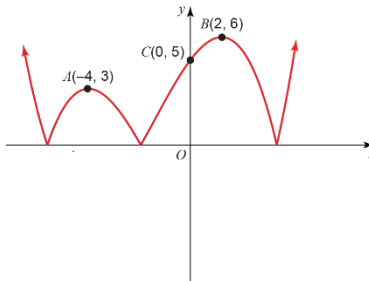
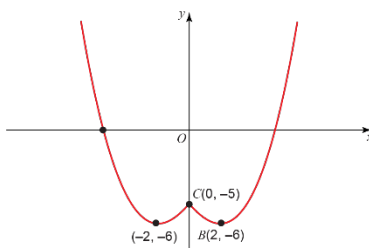
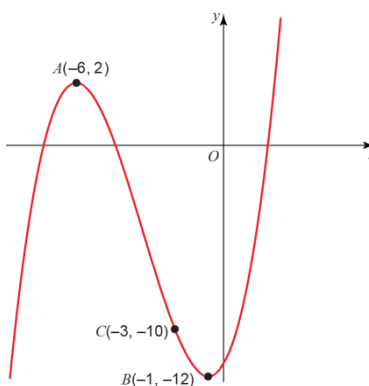


| Q | Scheme | | Marks | AOs | Pearson Progression Step and Progress descriptor |
|------------|---|---|-------|------|---|
| 1a | Figure 1  | Graph has a distinct V-shape. | M1 | 2.2a | 5th Sketch the graph of the modulus function of a linear function. |
| | | Labels vertex $\left(-\frac{3}{2}, -4\right)$ | A1 | 2.2a | |
| | | Finds intercept with the y-axis. | M1 | 1.1b | |
| | | Makes attempt to find x-intercept, for example states that $ 2x + 3 - 4 = 0$ | M1 | 2.2a | |
| | | Successfully finds both x-intercepts. | A1 | 1.1b | |
| | | | (5) | | |
| 1b | Recognises that there are two solutions. For example, writing $2x + 3 = -\frac{1}{4}x + 2$ and $-(2x + 3) = -\frac{1}{4}x + 2$ | | M1 | 2.2a | 5th Solve equations involving the modulus function. |
| | Makes an attempt to solve both questions for x, by manipulating the algebra. | | M1 | 1.1b | |
| | Correctly states $x = -\frac{4}{9}$ or $x = -\frac{20}{7}$. Must state both answers. | | A1 | 1.1b | |
| | Makes an attempt to substitute to find y. | | M1 | 1.1b | |
| | Correctly finds y and states both sets of coordinates correctly $\left(-\frac{4}{9}, -\frac{17}{9}\right)$ and $\left(-\frac{20}{7}, -\frac{9}{7}\right)$ | | A1 | 1.1b | |
| | | | (5) | | |
| (10 marks) | | | | | |
| Notes | | | | | |

| Q | Scheme | Marks | AOs | Pearson Progression Step and Progress descriptor |
|---|---|------------|------|--|
| 2a | States or implies that $pq(x) = (5 - 2x)^2$ | M1 | 2.2a | 5th Find composite functions. |
| | States or implies that $qp(x) = 5 - 2x^2$ | M1 | 2.2a | |
| | Makes an attempt to solve $(5 - 2x)^2 = 5 - 2x^2$. For example, $25 - 20x + 4x^2 = 5 - 2x^2$ or $6x^2 - 20x + 20 = 0$ is seen. | M1 | 1.1b | |
| | States that $3x^2 - 10x + 10 = 0$. Must show all steps and a logical progression. | A1 | 1.1b | |
| | | (4) | | |
| 2b | $b^2 - 4ac = 100 - 4(3)(10) = -20 < 0$ | M1* | 2.2a | 5th Find the domain and range of composite functions. |
| | States that as $b^2 - 4ac < 0$ there are no real solutions to the equation. | B1* | 3.2b | |
| | | (2) | | |
| (6 marks) | | | | |
| <p style="text-align: center;">Notes</p> <p>2b</p> <p>Alternative Method</p> <p>M1: Uses the method of completing the square to show that $3\left(x - \frac{5}{3}\right)^2 + \frac{65}{9} = 0$ or $3\left(x - \frac{5}{3}\right)^2 = -\frac{65}{9}$</p> <p>B1: Concludes that this equation will have no real solutions.</p> | | | | |

| Q | Scheme | Marks | AOs | Pearson Progression Step and Progress descriptor |
|------------------|--|------------|------|--|
| 3a | Makes an attempt to find $fg(x)$. For example, writing $fg(x) = e^{2\ln(x+1)} + 4$ | M1 | 2.2a | 5th Find composite functions. |
| | Uses the law of logarithms to write $fg(x) = e^{\ln(x+1)^2} + 4$ | M1 | 1.1b | |
| | States that $fg(x) = (x+1)^2 + 4$ | A1 | 1.1b | |
| | States that the range is $y > 4$ or $fg(x) > 4$ | B1 | 3.2b | |
| | | (4) | | |
| 3b | States that $(x+1)^2 + 4 = 85$ | M1 | 1.1b | 5th Find the domain and range of composite functions. |
| | Makes an attempt to solve for x , including attempting to take the square root of both sides of the equation. For example, $x+1 = \pm 9$ | M1 | 1.1b | |
| | States that $x = 8$. Does not need to state that $x \neq -10$, but do not award the mark if $x = -10$ is stated. | A1 | 3.2b | |
| | | (3) | | |
| (7 marks) | | | | |
| Notes | | | | |

| Q | Scheme | Marks | AOs | Pearson Progression Step and Progress descriptor |
|-----------|--|-------|------|--|
| 4 | Understands the need to complete the square, and makes an attempt to do this. For example, $(x-4)^2$ is seen. | M1 | 2.2a | 6th Find the domain and range of inverse functions. |
| | Correctly writes $g(x)=(x-4)^2-9$ | A1 | 1.1b | |
| | Demonstrates an understanding of the method for finding the inverse is to switch the x and y . For example, $x=(y-4)^2-9$ is seen. | B1 | 2.2a | |
| | Makes an attempt to rearrange to make y the subject. Attempt must include taking the square root. | M1 | 1.1b | |
| | Correctly states $g^{-1}(x)=\sqrt{x+9}+4$ | A1 | 1.1b | |
| | Correctly states domain is $x>-9$ and range is $y>4$ | B1 | 3.2b | |
| (6 marks) | | | | |
| Notes | | | | |

| Q | Scheme | | Marks | AOs | Pearson Progression Step and Progress descriptor |
|-----------|--|--|-------|------|--|
| 5a | Figure 2  | Clear attempt to reflect the negative part of the original graph in the x -axis. | M1 | 2.2a | 7th Sketch the graphs of the modulus function of unfamiliar non-linear functions. |
| | | Labels all three points correctly. | A1 | 1.1b | |
| | | Fully correct graph. | A1 | 1.1b | |
| | | | (3) | | |
| 5b | Figure 3  | Clear attempt to reflect the positive x part of the original graph in the y -axis. | M1 | 2.2a | 7th Sketch the graphs of the modulus function of unfamiliar non-linear functions. |
| | | Labels all three points correctly. | A1 | 1.1b | |
| | | Fully correct graph. | A1 | 1.1b | |
| | | | (3) | | |
| 5c | Figure 4  | Clear attempt to move the graph to the left 3 spaces. | M1 | 2.2a | 6th Combine two or more transformations, including modulus graphs. |
| | | Clear attempt to stretch the graph vertically by a factor of 2. | M1 | 2.2a | |
| | | Fully correct graph. | A1 | 1.1b | |
| | | | (3) | | |
| (9 marks) | | | | | |
| Notes | | | | | |

| Q | Scheme | Marks | AOs | Pearson Progression Step and Progress descriptor |
|------------------|--|--------------|------|--|
| 6a | States the range is $y \geq -5$ or $f(x) \geq -5$ | B1 | 3.2b | 5th Find the domain and range for a variety of familiar functions. |
| | | (1) | | |
| 6b | Recognises that $3(x-4)-5 = -\frac{1}{3}x+k$ and $-3(x-4)-5 = -\frac{1}{3}x+k$ | M1 | 2.2a | 7th Solve problems involving the modulus function in unfamiliar contexts. |
| | Makes an attempt to solve both of these equations. | M1 | 1.1b | |
| | Correctly states $\frac{10}{3}x = k+17$. Equivalent version is acceptable. | A1 | 1.1b | |
| | Correctly states $-\frac{8}{3}x = k-7$. Equivalent version is acceptable. | A1 | 1.1b | |
| | Makes an attempt to substitute one equation into the other in an effort to solve for k . For example, $x = \frac{3}{10}(k+17)$ and $-\left(\frac{8}{3}\right)\left(\frac{3}{10}\right)(k+17) = k-7$ is seen. | M1 ft | 2.2a | |
| | Correctly solves to find $k = -\frac{11}{3}$ | A1 ft | 1.1b | |
| | States the correct range for k . $k > -\frac{11}{3}$ | B1 | 3.2b | |
| | | (7) | | |
| (8 marks) | | | | |

Notes**6b**

Award ft marks for a correct method using an incorrect answer from earlier in the question.

Alternative Method

Student draws the line with gradient $-\frac{1}{3}$ passing through the vertex and calculates that $k = -\frac{11}{3}$, so answer is

$$k > -\frac{11}{3}$$

M1: States the x -coordinate of the vertex of the graph is 4

M1: States the y -coordinate of the vertex of the graph is -5

M1: Writes down the gradient of $-\frac{1}{3}$ or implies it later in the question.

M1: Attempts to use $y - y_1 = m(x - x_1)$ with $(x_1, y_1) = (4, -5)$ and $m = -\frac{1}{3}$

A1: Finds $y = -\frac{1}{3}x - \frac{11}{3}$ o.e.

B1: States the correct range for k : $k > -\frac{11}{3}$

| Q | Scheme | Marks | AOs | Pearson Progression Step and Progress descriptor |
|-----------|---|-------|------|---|
| 7a | Makes an attempt to substitute $t = 0$ into $T(t) = T_R + (90 - T_R)e^{-\frac{1}{20}t}$. For example, $T(t) = T_R + (90 - T_R)e^0$ or $T(t) = T_R + (90 - T_R)$ is seen. | M1 | 3.1a | 6th Set up and use exponential models of growth and decay. |
| | Concludes that the T_R terms will always cancel at $t = 0$, therefore the room temperature does not influence the initial coffee temperature. | B1 | 3.5a | |
| | | | (2) | |
| 7b | Makes an attempt to substitute $T_R = 20$ and $t = 10$ into $T(t) = T_R + (90 - T_R)e^{-\frac{1}{20}t}$. For example, $T(10) = 20 + (90 - 20)e^{-\frac{1}{20}(10)}$ is seen. | M1 | 1.1b | 6th Set up and use exponential models of growth and decay. |
| | Finds $T(10) = 62.457...^{\circ}\text{C}$. Accept awrt 62.5° . | A1 | 1.1b | |
| | | | (2) | |
| (4 marks) | | | | |
| Notes | | | | |